Variable selection worksheet

Friday, April 17, 2020 11:25 AM



Worksheet: Multiple Regression and Variable Selection

Part 1: What Not To Do. Party in power and economic performance.

Go to https://projects.fivethirtyeight.com/p-hacking/

(a) Suppose you are a Democratic data analyst with an agenda: You want to show that the economy performs better when Democrats are in power.

- Choose "Democrats" for the political party. The horizontal axis of the plot now measures the amount of power held by Democrats, and the vertical axis the performance of the economy. Your goal is to find statistically significant evidence of an association between these variables (p-value as small as you can make it), with a positive slope
- By changing the settings for which politicians are included, how economic performance is measured, and the options for weighting politicians by how powerful they are and whether or not recessions are excluded, manipulate the variables used until you have found statistically significant evidence of a positive association between these variables.

You win! Case proved, write it up and get published.

(b) Suppose you are a Republican data analyst with an agenda: You want to show that the economy performs better when Democrats are in power.

- Choose "Republicans" for the political party. The horizontal axis of the plot now measures the amount of power held by Republicans, and the vertical axis the performance of the economy. Your goal is to find statistically significant evidence of an association between these variables (p-value as small as you can make it), with a positive slope
- By changing the settings for which politicians are included, how economic performance is measured, and the options for weighting politicians by how powerful they are and whether or not recessions are excluded, manipulate the variables used until you have found statistically significant evidence of a positive association between these variables.

You win! Case proved, write it up and get published.

What's the point?

- You can find "statistically significant" evidence of anything if that is your goal and you are flexible enough in your data analysis. That doesn't mean your conclusions are correct.
- Formally, a p-value only measures the strength of evidence against the null hypothesis of the test if the analysis was pre-specified before looking at the data. If the test or the model you fit was dependent on the data in any way, the p-value is unreliable as an indicator of strength of evidence.
- Our goal is not to find statistically significant results. Our goal is to present an honest discussion of what the data can and cannot tell us about the world, complete with limitations of our analysis. A result is only convincing if it shows up in a variety of reasonable analyses of the data.
- We *must* present results from all reasonable models for the data based on a variety of reasonable decisions about what variables are included in the model and how those variables are defined.
- Any time someone has a really complicated data set and they present only a few findings from a single model, you should be very suspicious.

Part 2: What To Do. Nursing Salaries.

We have data about 52 licensed nursing home facilities in New Mexico, collected by the Department of Health and Social Services of the State of New Mexico. Let's use these data to estimate the relationship between the salaries of nurses at a given facility (NurseSalaries, our response variable) and a variety of other characteristics of the facility. The variables in the data set are:

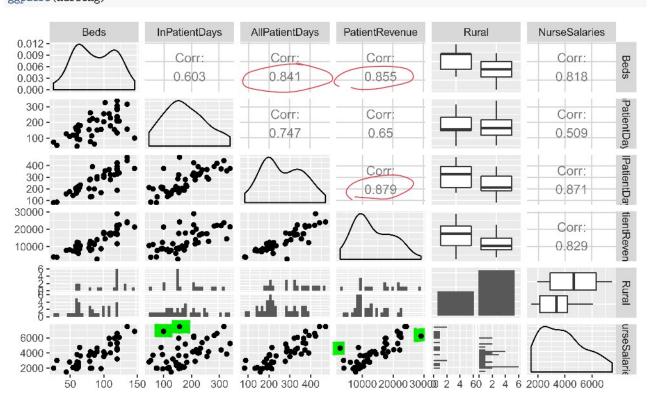
- Beds: Number of beds in the nursing home
- InPatientDays: Annual medical in-patient days (in hundreds)
- AllPatientDays: Annual total patient days (in hundreds)
- PatientRevenue: Annual patimet care revenue (in hundreds of dollars)
- Rural: Either "Rural" or "Non-Rural"
- NurseSalaries: Annual nursing salaries (in hundreds of dollars)

I have removed three outlying/high leverage observations. In order to focus on other aspects of the analysis, for today we will ignore these data points (ordinarily, we should check and see whether our conclusions depend on whether those observations are included).

##	#	A tibl	ole: 6 x 6				
##		Beds	${\tt InPatientDays}$	${\tt AllPatientDays}$	${\tt PatientRevenue}$	Rural	NurseSalaries
##		<dbl></dbl>	<db1></db1>	<db1></db1>	<dbl></dbl>	<chr></chr>	<db1></db1>
##	1	59	155	203	9160	Rural	2459
##	2	120	281	392	21900	Non-Rural	6304
##	3	120	291	419	22354	Non-Rural	6590
##	4	120	238	363	17421	Non-Rural	5362
##	5	65	180	234	10531	Rural	3622
##	6	120	306	372	22147	Rural	4406

Here is a pairs plot of the data.

library(GGally)
ggpairs(nursing)



1. Based on the pairs plot, perform an initial check of the conditions of linearity, equal variance, and
no outliers/high leverage observations. Also check and see whether there are any indications of potential
problems with multicollinearity.
Linearity: Looking at the last now, linearity Seems reasonable. The linearity: Looking at the last now, linearity Seems reasonable. The linear association is weakest for NurseSalaries versus InPatientDays Outliers Leverage There may be some influential points, shown in green. Equal variance: Chenerally this looks okay, There may be problems with
association is weakest for Nurse Salaries versus InPatient Days
when he come influential points shown in onein
Outliers Leverage There may be proliferny with
Equal variance: Chenerally this books thay, your may be of the
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InPatient Days.
highly correlated with Intattered buys
Multicollineauty: Blow to a Transferrithan and Patient Revenue also appear
Patient Kevenue. Input level Dag nation of multi-
Multicollinearity: Bedo are highly correlated with Infatient Days and Multicollinearity: Bedo are highly correlated with Infatient Days and Patient Revenue also appear to be highly correlated. These are potential sources of multi-collinearity.
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2. Based on the pairs plot, which of the explanatory variables appear to have the strongest association with nursing salaries?

All Patient Days, followed by Patient Revenue, and then Beds. These are all highly correlated with each other, too.

Here is a model that has NurseSalaries as the response, all other variables in the data set as explanatory variables, and does not include any interaction terms. Also shown are the variance inflation factors (VIF) for the coefficient estimates in this model.

```
lm_fit <- lm(NurseSalaries ~ Beds + InPatientDays + AllPatientDays + PatientRevenue + Rural, data = nursing)</pre>
summary(lm_fit)
##
## Call:
## lm(formula = NurseSalaries ~ Beds + InPatientDays + AllPatientDays +
      PatientRevenue + Rural, data = nursing)
##
##
## Residuals:
               1Q Median
                               3Q
##
      Min
                                      Max
## -1312.0 -480.3 -192.4
                            675.0 1698.1
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  51.95128 455.81747 0.114 0.90979
                  10.61995 7.16125 1.483 0.14537
## Beds
## InPatientDays -6.77619 2.23580 -3.031 0.00412 **
## AllPatientDays 13.21671
                           2.83591 4.660 3.05e-05 ***
## PatientRevenue 0.04464 0.03907
                                      1.142 0.25958
## RuralRural
                 -17.02622 252.20773 -0.068 0.94649
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 713.4 on 43 degrees of freedom
## Multiple R-squared: 0.8302, Adjusted R-squared: 0.8104
## F-statistic: 42.04 on 5 and 43 DF, p-value: 1.744e-15
vif(lm_fit)
            Beds InPatientDays AllPatientDays PatientRevenue
##
                                                                      Rural
```

3. Do the variance inflation factors indicate potential issues with multicollinearity? What does the VIF for Beds mean for the size of a confidence interval for β_1 in the model?

5.526630

1.387749

7.196287

##

4.380440

2.586838

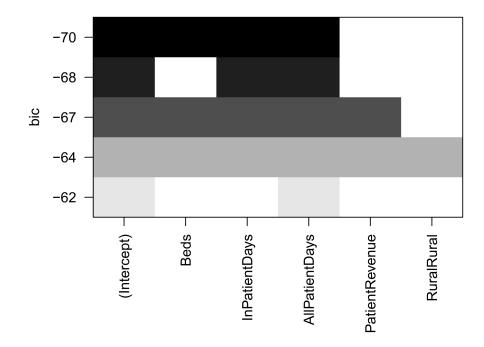
The VIFs for Beds, AllPatient Days, and Patient Revenue are all moderately large and indicate potential ussues with multicollinearity.

Multicollinearity negatively impacts the precision of our estimates. Therefore, the MF for Beds means that the confidence interval for β , in the model is too wide, confidence interval for β , in the model is too wide, relative to what it would be if we eliminated some nulticollinearity by removing correlated terms from the multicollinearity by removing correlated terms from the

4. Below are results from an all subsets regression. Based on these results, which models have roughly equivalent performance?

```
library(leaps)
## Warning: package 'leaps' was built under R version 3.6.3
candidate_models <- regsubsets(NurseSalaries ~ Beds + InPatientDays + AllPatientDays + PatientRevenue + Rural,
summary(candidate_models)
## Subset selection object
## Call: regsubsets.formula(NurseSalaries ~ Beds + InPatientDays + AllPatientDays +
      PatientRevenue + Rural, data = nursing)
##
## 5 Variables (and intercept)
                Forced in Forced out
##
## Beds
                    FALSE
                           FALSE
## InPatientDays
                    FALSE
                               FALSE
## AllPatientDays FALSE
                               FALSE
## PatientRevenue
                    FALSE
                               FALSE
## RuralRural
                    FALSE
                               FALSE
## 1 subsets of each size up to 5
## Selection Algorithm: exhaustive
          Beds InPatientDays AllPatientDays PatientRevenue RuralRural
                                                          " " Nurse Salaries ~ InPatient Days
## 1 (1) " " " "
## 2 ( 1 ) " " "*"
                                            H 11
## 3 (1) "*" "*"
## 4 ( 1 ) "*" "*"
## 5 (1) "*" "*"
                              "*"
                                            "*"
                                                          **
summary(candidate_models)$bic
## [1] -61.93374 -68.40657 -69.84360 -67.41191 -63.52529
plot(candidate_models)
```

Models 2,3, and 4 have roughly equal performance. Note none of these models includes all 3 correlated predictors previously identified.



5. Here are summaries of the model fits for the three best models in part 4. Summarize what these models have to say about the associations between the explanatory and response variables in the data set.

```
fit1 <- lm(NurseSalaries ~ InPatientDays + AllPatientDays, data = nursing)
summary(fit1)
##
## Call:
## lm(formula = NurseSalaries ~ InPatientDays + AllPatientDays,
      data = nursing)
##
##
## Residuals:
##
     Min
               1Q Median
                               3Q
                                      Max
## -1876.7 -479.6 -174.1 535.6 1590.9
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  172.858
                             313.889 0.551 0.58451
## InPatientDays
                   -7.137
                               2.168 -3.292 0.00192 **
                 18.712
                               1.649 11.348 6.28e-15 ***
## AllPatientDays
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 739.2 on 46 degrees of freedom
## Multiple R-squared: 0.8049, Adjusted R-squared: 0.7964
## F-statistic: 94.9 on 2 and 46 DF, p-value: < 2.2e-16
fit2 <- lm(NurseSalaries ~ Beds + InPatientDays + AllPatientDays, data = nursing)
summary(fit2)
## Call:
## lm(formula = NurseSalaries ~ Beds + InPatientDays + AllPatientDays,
##
      data = nursing)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -1345.6 -493.9 -231.6
                           678.0 1756.4
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  -95.948
                             322.976 -0.297 0.76778
## Beds
                   14.315
                               6.296
                                      2.274 0.02780 *
## InPatientDays
                   -6.804
                               2.081 -3.269 0.00207 **
## AllPatientDays
                  14.801
                               2.335 6.340 9.75e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 707.8 on 45 degrees of freedom
## Multiple R-squared: 0.825, Adjusted R-squared: 0.8134
## F-statistic: 70.72 on 3 and 45 DF, p-value: < 2.2e-16
fit3 <- lm(NurseSalaries ~ Beds + InPatientDays + AllPatientDays + PatientRevenue, data = nursing)
summary(fit3)
## Call:
## lm(formula = NurseSalaries ~ Beds + InPatientDays + AllPatientDays +
      PatientRevenue, data = nursing)
## Residuals:
      Min
               1Q Median
                               ЗQ
                                      Max
```

```
## -1318.2 -484.4 -198.6 669.8 1697.8
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept) 31.78007 340.30998 0.093 0.92602
## Beds
                  10.68348
                            7.01838 1.522 0.13511
                            2.07384 -3.293 0.00196 **
## InPatientDays -6.82842
## AllPatientDays 13.27368
                            2.67666 4.959 1.1e-05 ***
                            0.03854 1.154 0.25488
## PatientRevenue 0.04446
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 705.2 on 44 degrees of freedom
## Multiple R-squared: 0.8302, Adjusted R-squared: 0.8147
## F-statistic: 53.77 on 4 and 44 DF, p-value: < 2.2e-16

there is consistent violence across these three models that
 as the number of annual medical impatient days increases,
 nurse palary decreases. Conversely, there is consistent, strong evidence that as the annual total patient days increases, nurse salary also increases. There is no consistent evidence that beds or
  patient revenue are associated with nurse salary.
```